# 3-D Tunnel TiO<sub>2</sub> Crystal Phase as a Fast Charging Lithium Battery Anode from Stochastic Surface Walking-Based Material Screening

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**Supporting Information** 

**ABSTRACT:** To search for both high-rate capacity and high stability Li-ion battery anodes, here we design a new strategy of high-throughput material screening based on novel global potential energy surface exploration techniques. This permits us to quantify the structural evolution thermodynamics for 11 candidate materials after lithiation. When reaching the high capacity (~300 mA h/g) in lithiation, all bulk materials studied are shown to experience solid-to-solid phase transition with appreciable volume expansion. Among 11 candidates, we screen out a new three-dimensional (3-D) tunnel TiO<sub>2</sub> (TiO<sub>2</sub>-



S) phase to be a high-performance anode material. This  $TiO_2$ -S phase has a spinel-like structure, achieving only 5.5% volume expansion at 335.5 mA h/g capacity (Li +  $TiO_2 \rightarrow LiTiO_2$ ) and also possessing a fast charging kinetics as seen from the low Li diffusion barrier in a wide range of Li concentrations. Because all common stable forms of materials are not good anode materials at high-rate condition, our results indicate that metastable phases with 3-D open structures could be the choice for the next-generation Li-ion battery anode. A natural database for these candidates could be the delithiated crystal phases with open skeletons that are stable enough to survive in subsequent (dis)charging cycles.

## 1. INTRODUCTION

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Recent rapid developments in mobile electronic devices as well as electric vehicles demand better Li-ion batteries with high capacity, high-rate performance, and high stability.<sup>1-6</sup> The anode material is a major bottleneck for achieving the high performance considering that the common graphite cells suffer from low energy density (the engineering limit for the gravimetric capacity  $C_g$  is 372 mA h/g at LiC<sub>6</sub>) and low charging speed (the reversible capacity is ~370 mA h/g at the cycling current rate  $\sim C/24$ ).<sup>7</sup> While huge efforts have been made to search for better Li-ion anode materials, such as Li-M (M = Si, Ge, Sn, etc.) alloys<sup>8,9</sup> and lithium transition-metal oxide (i.e.,  $TiO_2$ ),<sup>10,11</sup> it is common to note that the charging to high capacities is often accompanied with massive volume expansion that destroys the structural integrity of the material, which involves complex solid reactions and phase transitions. This structural variation results in electrode pulverization, capacity fading, and limited cycling life as well as safety issues.<sup>12-14</sup> A key in designing reliable Li-ion battery anodes in fast charging is thus to identify the controlling factors that influence the structural integrity of the material, which requires a detailed knowledge on the mechanism of structural evolution during lithiation.

The structural deformation in lithiation is undesirable because solid-to-solid reactions are generally slow and inelastic (irreversible). Unfortunately, the volume expansion and the corresponding structural deformation have been commonly observed on most anode materials, especially at high capacity. For a traditional graphite anode, it is ~10% volume expansion at its capacity limit of LiC<sub>6</sub> (higher capacities are thermodynamically prohibited).<sup>15</sup> For the alloy anodes (Li<sub>x</sub>M), although they can exhibit remarkable ability to host Li (i.e., 4200 mA h/g for Li<sub>4.4</sub>Si, 1600 mA h/g for Li<sub>4.4</sub>Ge, and 900 mA h/g for Li<sub>4.4</sub>Sn) in theory, a massive volume expansion (>300%) and the crystal-to-amorphous phase transition can occur even in the first lithiation cycle at room temperature.<sup>16,17</sup> Advanced in situ techniques (e.g., X-ray diffraction and transmission electron microscopy) have confirmed the formation of solid solution Li<sub>x</sub>Si at the high capacities, as expected from thermodynamics,<sup>18,19</sup> which is responsible for the large volume expansion compared to that of Si.

 $\text{TiO}_2$  as an alternative material has received more attention because of its small volume expansion, better cyclability, and fast kinetics. Previous research<sup>20–23</sup> shows that (i) the maximum theoretical capacity, ~335 mA h/g (LiTiO<sub>2</sub>), can indeed be reached in specific samples, for example, <10 nm nanostructures for anatase.<sup>24</sup> (ii) The higher current rate is observed only at the relatively low capacity  $\text{Li}_{x(x\leq0.5)}$ TiO<sub>2</sub> (e.g.,

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~100 mA h/g at 30 C for anatase<sup>25,26</sup>). It was speculated that Li diffusion is kinetically restricted at the high Li intercalation condition, which should be affected by the lithium bonding environment in the TiO<sub>2</sub> lattice.<sup>21,27</sup> (iii) a number of Li<sub>x</sub>TiO<sub>2</sub> polymorphs (i.e., anatase, <sup>24,28</sup> spinel,<sup>29</sup> and ramsdellite<sup>30</sup>) have been synthesized via different methods in the experiment. From theoretical calculations,<sup>21</sup> anatase LiTiO<sub>2</sub> is found to be the most stable among eight possible polymorphs of LiTiO<sub>2</sub> (rutile, anatase, brookite, TiO<sub>2</sub>–B, ramsdellite, hollandite, spinel, and hexagonal). However, whether there are new TiO<sub>2</sub> phases with high performance in the Li-ion battery remains unknown.

Obviously, the lithiation-induced material degradation is a complex phenomenon influenced by many factors, for example, morphology, electronic structures (e.g., cohesive energy), and charging conditions (dynamics). The search for simple and robust parameters for the design of the better Li-ion battery represents a huge challenge to the field. In fact, the major problem in materials design is that the properties (volume, capacity, and stability) of the lithiated product  $Li_nX$  (X +  $nLi^+$  $+ ne^- \rightarrow Li_n X$ ) are generally unknown a priori because of the lack of knowledge on the atomic structure and chemical composition. It would be desirable to establish a highthroughput method to achieve the material screening. However, because of the slow kinetics of solid reactions, the traditional simulation tools, for example, molecular dynamics, have been frustrated for studying solid systems involving phase transitions because of the limited time scale in simulation. New theoretical tools are thus called for, which need to explore efficiently the likely lithiated solid phases and establish the global potential energy surface (PES). With the atomic structures of the thermodynamically stable lithiated product Li<sub>n</sub>X, one would expect that the search for high-performance anode materials can be accelerated significantly.

## 2. METHODS

Here, we propose a three-step screening strategy to identify a better Li-ion anode material as shown in Scheme 1, namely,

Scheme 1. Three-Step Screening Strategy (Coarse Screening, Fine Screening, and Property Assessment) To Identify Better Li-Ion Anode Materials<sup>a</sup>



"SSW–DFT: first-principles-based SSW Global optimization. SSW– NN: SSW Global optimization using NN potential.

coarse screening, fine screening, and property assessment. Our method starts with a coarse screening step using the first principles-based stochastic surface walking (SSW) global optimization method [SSW-density functional theory (DFT)]<sup>31-33</sup> to select potential candidates. The SSW global optimization has demonstrated the power in exploring solid phases and quantifying the phase transition kinetics.<sup>34,35</sup> This allows us to follow the complex solid phase transition trajectory in a high-throughput manner. We then utilize the fine screening procedure to focus on the promising candidates  $(e.g., LiTiO_2)$  using the latest machine-learning approach as implemented in the LASP code, that is, SSW-NN method<sup>36-40</sup> that combines the global neural network (NN) potential with the SSW method to explore the desirable composition ( $Li_x TiO_2$  at different x ratios).With SSW-NN global search, one can routinely search for 10<sup>7</sup> structures on global PES for systems up to 100 atoms per cell and cover all likely compositions. At the final stage, the property assessment is utilized to evaluate the anode performance. The detail of the method and the calculation setup can be found in the Supporting Information. It should be mentioned that firstprinciples DFT calculations have been utilized to validate the low energy structures and confirm the identified global minimum (see the Supporting Information for details on DFT calculations). All energetics reported here are from DFT without specifically mentioning.

# 3. RESULTS

3.1. Coarse Screening. Our first-stage coarse screening is carried out as follows. We have explored the PES of lithiated materials with the Li/X ratio = 1 for 11 candidates with X being C (graphite), Si (cubic), Ag (fcc), Al (fcc), As (trigonal), Ge (cubic), Zn (cubic), Au (fcc), Sn (cubic), SnO<sub>2</sub> (tetragonal), and TiO<sub>2</sub> (anatase). The starting phase/structure of X in SSW exploration is indicated in parenthesis, which is utilized as the energy reference for pure material. The specific Li/X = 1 ratio is selected for two reasons: (i) it can yield the capacity above 300 mA h/g in general, the limiting capacity of graphite, which is naturally set as the minimum target to achieve and (ii) the simulation with this ratio can be carried out in relatively small supercells in periodic calculations, which can significantly expedite the PES exploration. It should be emphasized that the first-stage coarse screening is not aimed for finding the exact global minimum nor exploring exhaustively the PES of the target material but for selecting the potential candidates with good structure integrity. It is thus achievable within a reasonable short time even with firstprinciples-based SSW global optimization (e.g., using relatively small unit cells).

To analyze the large dataset obtained from SSW global optimization, we have introduced a new quantity,  $dC_{g-V}$ , that is the gravimetric capacity ( $C_g$ ) per volume expansion percentage (dV %), as derived below.

$$dV\% = [(V - V_{\rm ref})/V_{\rm ref}] \times 100$$
 (1)

$$\mathrm{d}C_{\mathrm{g-V}} = C_{\mathrm{g}}/\mathrm{d}V \ \% \tag{2}$$

where V is the volume of  $\text{Li}_n X$ ,  $V_{\text{ref}}$  is the volume of starting X as the reference, and dV % is the percentage of volume expansion after lithiation. Obviously, a good anode material should have both a large  $C_{\text{g}}$  and a large  $dC_{\text{g-V}}$ , representing a high power density with a low volume expansion after lithiation. On the other hand, the formation energy  $\Delta E_{\text{f}}$  (eV

per formula unit, f.u.) reflects the thermodynamics of lithiation with reference to the bulk Li metal and the bulk X, given by  $\Delta E_{\rm f} = E_{{\rm Li}_{*X}} - nE_{{\rm Li}} - E_{X}$ , which can be further related to the open-circuit voltage  $V_0$  via the Nernst equation,  $V_0 = -\Delta E_{\rm f}/nF$ (*F*: Faraday constant). For the ideal anode,  $V_0$  should be positive but close to zero in order to yield the high output voltage. By using d $C_{\rm g-V}$  and  $\Delta E_{\rm f}$  as two key measures, we are able to fast screen anode candidates: the promising ones should appear on the top-right corner in the d $C_{\rm g-V} \sim \Delta E_{\rm f}$  plot.

By plotting  $dC_{g-V}$  against  $\Delta E_f$  of the most stable LiX phases, Figure 1a shows that, interestingly, group IV<sub>A</sub> materials, C, Si,



**Figure 1.** (a)  $dC_{g.V}$  vs  $\Delta E_f$  plot for LiX materials (host phase X = C, Si, Ag, Al, As, Ge, Zn, Au, Sn, SnO<sub>2</sub>, and TiO<sub>2</sub>); (b) most stable structures for C, Si, Sn, and TiO<sub>2</sub> after lithiation together with the initial pure phases. Li: magenta balls; host phases: lines. Also see the Supporting Information for the structures of all other lithiated phases (Figure S1).

and Sn, outperform others at the low  $\Delta E_{\rm f}$  (-0.75 to 0 eV), while TiO<sub>2</sub> is the best at the medium  $\Delta E_{\rm f}$  region (~-1.70 eV), as guided by the dotted line. The group IV materials such as C and Si have relatively large  $C_{\rm g}$  than other materials, despite their large volume expansion. On the other hand, TiO<sub>2</sub> has a good  $C_{\rm g}$  and a low volume expansion, which thus produces the far higher d $C_{\rm g-V}$  (61 and 78 mA h/g) than others.

To provide deeper insights into the  $dC_{g-V} \sim \Delta E_f$  relation, we have analyzed in detail the structure after lithiation for these materials. In Figure 1b, we show the structures for the four representative materials C, Si, Sn, and TiO<sub>2</sub>. The structures for others are detailed in the Supporting Information (Figure S1). In general, we note that these most stable LiX phases can be divided into three categories according to their structural features: (i) tunnel structures, as represented by TiO<sub>2</sub> (also in SnO<sub>2</sub>, metals Ag, Au, Al, and Zn); (ii) layer structures, as represented by Si (also in Ge, Sn, and As); and (iii) solidsolution structure, as represented by C, where LiC is a mix of carbon dimers and Li atoms. From SSW global optimization, it is clear that the intercalation of Li atoms, driven by thermodynamics, tends to expand the volume of the host to fit into the new-coming Li, which leads to the solid phase transition from the dense structure of the host to the Liintercalated open phases. In the following, we describe in detail the lithiated products for the four materials.

 $TiO_2$ : it is generally known that  $LiTiO_2$  exists in various polymorphic modifications, such as anatase,<sup>23,41</sup> spinel,<sup>29</sup>

ramsdellite,<sup>30,42</sup> and orthorhombic.<sup>43,44</sup> Interestingly, the SSW method has determined two stable polymorphs for LiTiO<sub>2</sub> according to the thermodynamics: one in a spinel-like lattice of  $TiO_2$  (TiO<sub>2</sub>-S) and another in an anatase lattice  $(TiO_2-A)$ . For the most stable LiTiO<sub>2</sub> (in the TiO<sub>2</sub>-S lattice), it has a relatively low volume expansion after lithiation to LiTiO<sub>2</sub>, dV % = 5.5%, thus achieving the high  $dC_{g-V}$  (61 mA h/ g) even with a moderate  $C_g = 335.5$  mA h/g. For the less stable  $LiTiO_2$  (in the TiO<sub>2</sub>-A lattice), the volume expansion is lower (4.3%), and thus, the  $dC_{g-V}$  has increased to 78 mA h/g. LiTiO<sub>2</sub> with the anatase lattice is slightly less stable than that with the  $TiO_2$ -S lattice, 0.66 meV per  $TiO_2$  formula unit (f.u.).  $\Delta E_{\rm f}$  of them are relatively low, -1.70 eV, reflecting the large exothermicity of lithiation, which, on the other hand, implies the high stability of the lithiated product. For the structures with other TiO<sub>2</sub> lattices, for example, spinel, ramsdellite, and orthorhombic tunnel structures, their  $\Delta E_f$  are relatively higher, above -1.59. The  $\Delta E_{\rm f}$  in LiTiO<sub>2</sub> suggests that TiO<sub>2</sub> has a relatively lower output voltage compared to C, Si, and Sn materials.

The crystal structures for  $LiTiO_2$  in  $TiO_2$ -S and  $TiO_2$ -A lattices are highlighted in Figure 2 from different view angles.



**Figure 2.** Ball-and-stick representations of  $TiO_2$ -S (a,b) and  $TiO_2$ -A (c) structures after lithiation (LiTiO<sub>2</sub>) as identified from SSW–NN global search. Li atoms locate at the octahedral interstitial sites (Li–O bond ~2.1 Å) in both lattices. O: red balls; Ti: gray balls; Li: magenta balls.

Both lattices are three-dimensional (3-D) interlinked structures with tunnels. The TiO<sub>2</sub>-S crystal structure (space group C2/C) differs slightly from the common spinel structure in that a layer of TiO<sub>6</sub> octahedra per unit cell slips along [100] by half of the lattice length (as shown in Figure 2a,b and Supporting Information, Figure S2). It has a 3-D tunnel spinel-like crystal structure with a density of 3.82 g/cm<sup>3</sup>, 2.8% lower than that of anatase. For LiTiO<sub>2</sub> in the TiO<sub>2</sub>-A lattice, the optimized lattice constants are *a*, *b* = 4.08 Å, *c* = 8.48 Å,  $\alpha = \beta = \gamma = 90^{\circ}$  with the space group I4<sub>1</sub>/*amd*. These structural data are consistent with the experimental measurement of anatase-type LiTiO<sub>2</sub> by neutron diffraction.<sup>24</sup>

We must emphasize that the energy difference between two  $LiTiO_2$  ( $TiO_2$ -S and  $TiO_2$ -A lattices) is extremely small (0.66 meV per f.u.), suggesting that the thermodynamic-driven force to phase transition at the  $LiTiO_2$  stage is not huge. This would help to maintain the structural integrity in Li intercalation–deintercalation cycles. In particular, the newly identified  $TiO_2$ -S may show excellent stability and cycling performance because it is the most stable structure at the high Li composition condition.

Si:  $\Delta E_{\rm f}$  for forming LiSi is -0.31 eV, suggesting that the Si anode has a good output voltage. Unfortunately, the volume expansion at the LiSi product is huge, dV % = 70.7%, which in turn reduces the dC<sub>g-V</sub> despite its large C<sub>g</sub> = 957.1 mA h/g. Importantly, as shown in Figure 1b, the Li addition destroys a

significant number of Si–Si bonds in the Si crystal (diamond) and leads to the formation of Si layer structures.

C:  $\Delta E_{\rm f}$  for forming LiC is positive, indicating that such a high Li composition is thermodynamically prohibited. This is consistent with the general knowledge on the limiting  $C_{\rm g}$  of LiC<sub>6</sub> for graphite. The poor energetics can be attributed to the huge structural deformation. The LiC phase has the largest volume expansion percentage (dV % = 203.5%) among all materials. Only individual C–C dimers are present in the LiC phase and surrounded by intercalated Li atoms (Figure 1b).

Sn: the lithiation of Sn is similar to that of Si on many aspects.  $\Delta E_{\rm f}$  for forming LiSn is -0.66 eV, being 0.35 lower than that of Si. Because of the larger mass weight of Sn than that of Si, the capacity  $C_{\rm g}$  is lower for Sn. However, the  $dC_{\rm g-V}$  is similar with that of Si, because its volume expansion is in fact much lower, dV % = 15.1%. The most stable LiSn phase is also a layer structure with Li filling in between Sn layers (Figure 1b).

From the above results, we reveal that the lithiation to high capacity will weaken dramatically the bondings of the host material and induce the solid phase transition toward open structures. This thermodynamic trend implies that the high capacity and the low volume expansion are a pair of paradoxical properties. To circumvent the problem, an obvious means is to abandon the common stable forms of the material but search for metastable new forms with stable open structures. The delithiated phases with open skeletons could be the more natural choices provided that they are stable enough in subsequent (dis)charging cycles.

**3.2. Fine Screening.** Along this line, we go further to select  $TiO_2$  and Si for a fine screening, where their stepwise structural evolution during Li intercalation will be examined in detail. From Figure 1a,  $TiO_2$  and Si are the materials most likely to achieve a balanced performance with high capacity density and good stability. We focus on the lithiated products of Si and  $TiO_2$  at different stages of Li/X ratio, spanning from 0.5 to 3, including Li<sub>0.5</sub>TiO<sub>2</sub>, LiTiO<sub>2</sub>, Li<sub>2</sub>TiO<sub>2</sub>, and Li<sub>3</sub>TiO<sub>2</sub> for TiO<sub>2</sub> and Li<sub>0.5</sub>Si, Li<sub>0.75</sub>Si, LiSi, Li<sub>1.25</sub>Si, Li<sub>1.5</sub>Si, and Li<sub>2</sub>Si for Si.

While DFT-based SSW PES exploration is utilized for structure search in Li, Si systems, we combine the SSW method with the recently developed global NN potential to construct the global PES of Li, TiO<sub>2</sub> and to assess their structural evolution, not least because of great structural complexity in ternary Li<sub>x</sub>TiO<sub>2</sub> systems. Despite the added computational cost for the first-principles dataset generation, the SSW-NN method allows to fast obtain the global PES of LirTiO2 because the NN simulation is at least 3-4 orders of magnitude faster than DFT (the accuracy of NN computation in energy and force is comparable with that from DFT, see the Supporting Information). In this work, each composition of  $Li_rTiO_2$  is simulated in different unit cells from 12 to 64 atoms and explored to cover more than 10 000 minima on PES by SSW [the calculation detail and our benchmark between DFT and the NN potential for Li<sub>x</sub>TiO<sub>2</sub> are shown in Supporting Information (Table S1)]. From the SSW-NN simulation, a large variety of Li<sub>x</sub>TiO<sub>2</sub> structures ranging from crystalline to amorphous structures are obtained, from which the stable polymorphs are determined by further DFT validation. By analyzing the collected most stable structure for each composition (see geometrical structures in Supporting Information, Figures S3 and S4), we can see that with the gradual intercalation of Li to the electrode framework, the original network of the host is weakened and broken that

eventually results in the formation of small clusters of the host material surrounded by Li ions. The most stable structures of the TiO<sub>2</sub> electrode exhibit the spinel (Li<sub>0.5</sub>TiO<sub>2</sub>), TiO<sub>2</sub>-S (LiTiO<sub>2</sub>), and layer structures successively with the increase of Li intercalation. For the Si electrode, the crystalline– amorphous evolution can be clearly observed as the Li contents increase.<sup>18,45,46</sup> The structure evolution of Si follows the pattern from the diamond matrix (Li<sub>0.5</sub>Si) to the sheets of the hexatomic ring (LiSi) and to a zigzag chain (Li<sub>2</sub>Si).

Three major trends are found from the volume and energetics data of these Li intercalated phases. First, with the increase of Li/X ratio, the volume for both systems increases gradually, as shown by the volume versus Li/X ratio plot in Figure 3a. Interestingly, we found that the volume of  $TiO_2$ 



**Figure 3.** (a) Volume (mL/mol) of Si and TiO<sub>2</sub> after lithiation; (b) formation energy ( $\Delta E_f$ ) convex hull of Si and TiO<sub>2</sub> at varied Li fraction y (Li<sub>y</sub>X<sub>1-y</sub>); (c) stability ( $\Delta E_{de}$ ) for delithiated TiO<sub>2</sub> and Si phases at varied Li fraction.

increases however marginally at the initial stage of low Li/X ratios ( $\leq$ 1). We found that this is caused by the polymorphism of 3-D tunnel TiO<sub>2</sub> phases that are able to accommodate Li ions at the low concentrations. The 3-D tunnel structure can be created by reducing the O anion coordination as reflected by the appearance of two-coordinated O in the bulk (see Figure 2). The volume versus Li/X ratio curves at the large ratios becomes very similar, although Si and TiO<sub>2</sub> are very different in bonding nature. The slope of both linear lines is close to the density of the Li metal (13.0 mL/mol per Li atom). The volume for the predicted LiSi phase (20.6 mL/mol) is consistent with the experimental result at about the same ratio (~19 mL/mol),<sup>47</sup> which validates our theoretical prediction for the LiSi phases.

Second, the formation energy  $\Delta E_{\rm f}$  for both Si and TiO<sub>2</sub> lithiation exhibits the typical convex hull with the increase of Li fraction y in the lattice  $(\text{Li}_y X_{1-y})$  as shown in Figure 3b. The largest  $\Delta E_{\rm f}$  occurs at the Li fraction of 0.5–0.8 for TiO<sub>2</sub> phases, while it is 0.6–0.7 for Si phases. They are the thermodynamically preferred phases after lithiation. The  $\Delta E_{\rm f}$ for the lithiation of TiO<sub>2</sub> is consistently larger than that of Si,

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which can be explained by the strong ionic character of Li-O bonds that are present in the lithiated  $TiO_2$ .

Third, the delithiated structures for TiO<sub>2</sub> are generally more stable than those for Si, especially when the Li fraction is larger than 0.45 as shown in Figure 3c. The energy change after Li depletion  $\Delta E_{de}(eV/f.u.)$  that measures the material stability after discharging is defined as  $\Delta E_{de} = E_{X'} - E_X$ , where  $E_{X'}$  is the total energy from DFT for the skeleton X generated from Li<sub>n</sub>X by relaxing Li-removed skeleton X while keeping the volume. The lower the  $\Delta E_{de}$ , the more stable the delithiated phase will be. From Figure 3c, it can be seen that TiO<sub>2</sub> is particularly advantageous to achieve a high stability with high Li contents.

**3.3. Property Assessment.** Taking  $\text{TiO}_2$  as the target material, we have finally investigated the (dis)charging kinetics for Li diffusion inside the  $\text{TiO}_2$  tunnel. The migration paths for LiTiO<sub>2</sub>-S/A and Li<sub>0.5</sub>TiO<sub>2</sub>-S/A have also been studied by creating one Li vacancy in the Li<sub>x</sub>TiO<sub>2</sub> crystal and determining the lowest energy pathway for Li diffusion from the neighboring site to this vacancy.

As shown in Figure 4 (also in Supporting Information, Figure S5), we found that the Li diffusion barrier ( $E_a$ : 0.55 eV)



Figure 4. Lowest energy pathway of Li diffusion in (a)  $TiO_2$ -S and (b)  $TiO_2$ -A at different Li concentrations.

in the fully lithiated TiO<sub>2</sub>-S structure (LiTiO<sub>2</sub>) is not much different from the corresponding dilute Li<sub>0.5</sub>TiO<sub>2</sub> (0.53 eV). This suggests that TiO<sub>2</sub>-S would maintain the high rate even at high capacity. The presence of the 3-D tunnel in TiO<sub>2</sub>-S plays the key role for the Li migration channel, which is critical for the purpose of fast charging. For the anatase crystal (TiO<sub>2</sub>-A), however, the Li diffusion barrier increases noticeably from 0.59 to 1.34 eV with the increase of Li content from Li<sub>0.5</sub>TiO<sub>2</sub> to LiTiO<sub>2</sub>. This result is consistent with the previous calculations (~0.50 eV for Li<sub>0.5</sub>TiO<sub>2</sub> and 1.37 eV for LiTiO<sub>2</sub>)<sup>48,49</sup> and experimental measurement (~0.5–0.6 eV for Li<sub>~0.5</sub>TiO<sub>2</sub><sup>48,50</sup>).

The difference in the barrier between pathways may be understood from the structure of the diffusion pathway. When Li diffuses out from one octahedral site, the two oxygen atoms of octahedral apexes have to be lengthened to allow Li to pass through. Because of the elongation of the O–O distance that weakens the original Ti–O bonding, it creates the barrier for Li diffusion. We found that the O–O distance increases by ~0.28 Å for the LiTiO<sub>2</sub>-S structure and ~0.25 Å for Li<sub>0.5</sub>TiO<sub>2</sub>-S and Li<sub>0.5</sub>TiO<sub>2</sub>-A but much higher, ~0.4 Å (from 3.0 to 3.4 Å), for LiTiO<sub>2</sub>-A during Li diffusion. This change in distance is in accordance with the computed diffusion barrier heights. For the LiTiO<sub>2</sub>-S structure, we found that all Li-occupying octahedral sites are distorted because of the presence of the 3-D tunnel structure, where the O–O distance varies from 2.9 to 3.2 Å. However, in LiTiO<sub>2</sub>-A, Li can distribute rather uniformly in the anatase skeleton with an O–O distance of 2.9–3.0 Å. The high barrier in LiTiO<sub>2</sub>-A can thus be attributed to the small octahedral distortion as suggested previously.<sup>49</sup>

$$j = nFA \exp(-E_a/RT)/m_{(TiO_2)}$$
(3)

From microkinetics, we can estimate the rate (j) of Li charging based on eq 3, where A is the pre-exponential factor (here, it is set as a typical value of  $10^{12}$ ),  $E_a$  is the diffusion barrier, and *m* is the mass weight of TiO<sub>2</sub>. In LiTiO<sub>2</sub>-S, the rate is estimated to be ~450 C, corresponding to ~8 s of charging/discharging. In contrast, the formation of the fully lithiated LiTiO<sub>2</sub>-A is kinetically inhibited with a very low rate, ~ $10^{-11}$  C.

Experimentally, while nanoporous structures are known to improve the (dis)charging performance of lithium-ion batteries, <sup>51,52</sup> only recently the interconnected framework composed of ultrasmall spinel nanocrystals of a few nanometers in size (Li<sub>4</sub>Ti<sub>5</sub>O<sub>12</sub> spinel) has been synthesized and exhibits a high-rate performance of ~130 mA h/g at 800 C.<sup>53</sup> While the crystal Li<sub>4</sub>Ti<sub>5</sub>O<sub>12</sub> is not exactly the same with our predicted crystal LiTiO<sub>2</sub>-S, the experiment evidence together with our results do suggest that the (spinel) tunnel crystal structure of TiO<sub>2</sub> can have the superior performance for the Liion battery, especially on the fast charging kinetics.

## 4. CONCLUSIONS

This work proposes a general strategy for high-throughput computational screening of the anode material based on the efficient global PES exploration. To demonstrate the approach, we select 11 different materials and study their structural evolution after lithiation. From the large dataset of lithiated phases, we find that the common carbon anode and silicon anode suffer from large  $C_g$  loss because of the massive volume expansion after lithiation, which is in fact intrinsic to most bulk materials. A new TiO<sub>2</sub> phase with a 3-D spinel-like tunnel structure that can in situ be produced during lithiation is discovered to be a high-performance anode material. The general rules for material structural deformation revealed here should be applicable for understanding the experimental findings and guiding the development of new anode materials.

## ASSOCIATED CONTENT

#### **Supporting Information**

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcc.9b04604.

SSW global structure search, SSW global PES exploration using NN potential, and DFT calculations; structure gallery of  $\text{Li}_x$ X phases; and Cartesian atomic coordinates of  $\text{Li}_x$ X phases (PDF)

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## Notes

The authors declare no competing financial interest.

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